

# NUMERICAL ANALYSIS

## FINAL EXAM

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ABSTRACT. The solution to each problem consists of two files: a C or C++ program (.C or .CPP extension), and output from that program (.TXT extension). You may use and modify the programs found at [www.saumag.edu/pbailey](http://www.saumag.edu/pbailey).

Submit solutions by email to [plbailey@saumag.edu](mailto:plbailey@saumag.edu) dated on or before Tuesday, December 9, 2003.

**Problem 1.** Start with the program `Matrix.cpp`. Recall that the determinant of an upper diagonal matrix is the product along the diagonal. Add a function to compute the determinant of a matrix by first applying the function `RowEch`. Find and print the determinant and the inverse of the matrix

$$A = \begin{bmatrix} 3 & 4 & 2 & 7 \\ 2 & 3 & 3 & 2 \\ 5 & 7 & 3 & 9 \\ 2 & 3 & 2 & 3 \end{bmatrix}.$$

**Problem 2.** Start with the program `Integ.cpp`. Let  $f(x) = \frac{2}{1+x^2}$ . For  $n \in \{1, 2, 4, 8, 16, 32\}$ , estimate  $\int_{-1}^1 f(x) dx$  using the midpoint rule, the trapezoidal rule, and Simpsons rule. Display the results in a grid for easy comparison.

**Problem 3.** Start with the program `Spline.cpp`. Consider the following table of points, derived from the function  $f(x) = \frac{2}{1+x^2}$ .

i	0	1	2	3	4	5	6
x	-3	-2	-1	0	1	2	3
y	$\frac{1}{5}$	$\frac{2}{5}$	1	2	1	$\frac{2}{5}$	$\frac{1}{5}$

Let  $p(x)$  be the Lagrange interpolation polynomial,  $s_1(x)$  the degree one spline, and  $s_2(x)$  the degree two spline corresponding to this table. Compute  $f(x)$ ,  $p(x)$ ,  $s_1(x)$ , and  $s_2(x)$  for the values  $a + kh$  for  $a = -4$ ,  $h = 0.4$ , and  $k = 0, 1, \dots, 20$ . Print these functions. Display the results in a grid for easy comparison.

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